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A method for aggregating external operating conditions in multi-generation plant optimization models

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Abstract

This paper presents a novel, simple method for reducing external operating condition datasets to be used in multi-generation plant optimization models. The method, called the Characteristic Operating Pattern (CHOP) method, is a visually-based aggregation method that clusters reference data based on parameter values rather than time of occurrence, thereby preserving important information on short-term relations between the relevant operating parameters. This is opposed to commonly used methods where data are averaged over chronological periods (months or years), and extreme conditions are hidden in the averaged values.

The CHOP method is tested in a case study where the operation of a fictive Danish combined heat and power plant is optimized over a historical 5-year period. The optimization model is solved using the full external operating condition dataset, a reduced dataset obtained using the CHOP method, a monthly-averaged dataset, a yearly-averaged dataset, and a seasonal peak/off-peak averaged dataset. The

economic result obtained using the CHOP-reduced dataset is significantly more accurate than that obtained using any of the other reduced datasets, while the calculation time is similar to those obtained using the monthly averaged and seasonal peak/off-peak averaged datasets. The outcomes of the study suggest that the CHOP method is advantageous compared to chronology-averaging methods in reducing external operating condition datasets to be used in the design optimization models of flexible multi-generation plants.

Keywords

Data aggregation; flexibility; multi-generation; operation optimization; polygeneration.

Nomenclature

Latin letters

C	Cost [Euro]
C_v	Power-to-heat production ratio [-]
c	Specific cost [Euro/MWh]
D	Dataset
F	Fuel consumption [MWh]
N	Number of groups
n	Number of characteristic parameter intervals
O	Operating point
P	Power [MWh]
p	Operating condition parameter
Q	Heat [MWh]
T	Time of occurrence
t	Duration [h]

Greek letters

α	Back-pressure ratio [-]
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47	λ	Load [-]
48	σ	Standard deviation [-]
49	Subscripts	
50	aa	Annually averaged
51	i	Characteristic parameter interval index
52	j	Data point index
53	k	EOC parameter index
54	l	CHOP group index
55	ma	Monthly averaged
56	pot	Potential
57	sp	Seasonal peak/off-peak averaged
58	Superscripts	
59	*	Linearized
60	Abbreviations	
61	CHOP	Characteristic operating pattern
62	CHP	Combined heat and power
63	EOC	External operating condition
64	FMG	Flexible multi-generation plant

65 **1. Introduction**

66 Large-scale integration of intermittent renewable energy sources (solar, wind, tidal and wave) in the energy
67 system imposes a demand for production-consumption balancing [1]. Flexible multi-generation plants
68 (FMGs), here defined as flexibly operating facilities integrating the production of two or more energy
69 services (power, heating, cooling, fuels etc.), may provide such balancing operation [2]. Furthermore, FMGs
70 based on biomass may achieve high aggregated biomass conversion efficiencies through process
71 integration [3], which is of crucial importance in sustainable energy systems as the biomass resource is

72 limited on a global level [4] [5]. Such process integration advantages may further be used for providing
73 sustainable fuel and energy services in FMGs at competitive prices [6] [7] [8], thereby integrating various
74 layers of the energy system. The development of efficient biomass-processing FMGs may therefore be seen
75 as an integral part of the transition towards a smart energy system based on renewable energy sources [9]
76 [10].

77 The design optimization of FMG concepts includes such challenges as synthesising processes from multiple
78 technological alternatives, facility and process dimensioning, process integration, feedstock market-impacts,
79 operation optimization etc. In addition to this, a principal challenge is to optimize design and operational
80 performance with respect to hourly fluctuations as well as long-term changes in demands and prices of
81 various energy products. In principle, these data could be obtained by implementing a detailed energy
82 system model [11] in the design optimization model, but the required data sampling, modelling, and
83 computational effort can be prohibitive. It is therefore common to include external operating conditions
84 (EOCs) that are hardly influenced by plant operation, such as fuel price, heating demand etc., as fixed
85 parameters in multi-period design optimization models. In a case study of a thermal energy system,
86 Hindsberger and Ravn [12] demonstrated that robust results can be obtained by using fixed EOC datasets
87 when external conditions are little affected by system operation.

88 A fundamental issue in mathematical optimization models is the trade-off between level of detail and ease
89 of solving the model. As the complexity of multi-period optimization problems increases significantly with
90 the number of periods defined [13], it is desirable to reduce the number of period datasets without
91 plummeting result accuracy. One approach to reducing the number of periods is to average EOC parameter
92 values over chronological time-periods. Among averaging methods, the simplest is to average the EOCs
93 over the lifetime of the plant (e.g. Ahmadi et al. [14], Gassner and Maréchal [15], and Chen et al. [16]). A
94 related method is to assume annually static operating conditions, but defining each year as a period to
95 allow for year-to-year variations caused by general energy system developments (e.g. Gerogiorgos et al.
96 [17], and Liu et al. [18] [19]). Another method is to consider monthly average values for one key operating

parameter and static conditions for all other (e.g. Fazlollahi et al. [20] [21]). A more detailed approach is to consider monthly averaged EOC parameter values in a first-step optimization model, and then conduct detailed hour-wise operation optimization in a sequential step for the most promising designs (e.g. Rubio-Maya et al. [22] and Uche et al. [23]). However, neither monthly- nor annually-averaged operating parameter values provide information on short-term relations and variations between various operating conditions. While it may be acceptable to neglect this information for static operating facilities, it can be critical to the economy and thermodynamic performance of flexible facilities such as combined heat and power (CHP) plants [24] and FMGs [25] [26]. Failing to consider short-term relations between relevant operating parameters may lead to sub-optimal solutions in the design optimization of FMGs [27].

One approach to reduce energy system data while maintaining details on hourly parameter relations is to represent each year by a small number of typical time-periods. Another approach is to define a number of characteristic periods, like peak-demand and off-peak-demand periods in each of the four seasons (e.g. Chen et al. [2] [28]) or typical demand days for each month based on monthly average parameter values (e.g. Mavrotas et al. [29]). These approaches rely on the assumption that operating conditions and energy demands are linked and cyclic over the seasons, an assumption that may prove inaccurate in energy systems in transition and with large shares of intermittent renewable energy production [1]. To overcome the assumption of cyclic behavior, several studies propose application of cluster analysis to identify typical periods that can be repeated in order to approximate the annual cumulative curves. Ortega et al. [30] proposed a graphical method for selecting a few typical days that can be used for representing the annual cumulative heating and cooling demand curves. Domínguez-Muñoz et al. [31] and Fazlollahi et al. [32] used a partitional clustering analysis method, the k -Medoids method, to create k typical periods. However, such approaches may hide information on peak and extreme operating conditions and lead to significant errors on peak operation performance, as also reported by Fazlollahi et al. [32] in two illustrative examples. In order to overcome these drawbacks, the duration of the typical periods may be extended to several consecutive days or even weeks (e.g. Hedegaard and Münster [33]). However, this approach increases the

computational effort significantly, thereby counteracting the initial ambition of reducing the number of period datasets. Instead, Bungener et al. [34] proposed a method that applied an evolutionary multi-objective optimization algorithm for identifying n sequential periods representing typical operations for an industrial cluster with the aim of minimizing standard deviation and, at the same time, maintain information on extreme operating conditions. Nemet et al. [35] presented a similar method for aggregating continuous thermal energy production and demand into sequential periods. They presented an MILP model for determining the number and duration of the periods required to obtain a certain level of accuracy over the aggregation. Karlsson et al. [36] proposed a simple method, called the TimeSlicesTool, which sorts annual operating points into three groups for critical combinations of operating characteristics and one group for all other operating points. This was done for work and non-work days in each of the four seasons, resulting in 32 groups. A drawback of this method is the fact that only information on extreme conditions is sustained, while detailed information on frequently occurring operating patterns is lost.

The present paper proposes a novel and simple aggregation-based method for reducing EOC datasets in optimization models. The method, named Characteristic Operating Pattern (CHOP) method, is tailored for reducing EOC datasets with non-cyclic behaviour for FMG optimization models, but it may be used for reducing similar datasets for any facility operating in multiple energy markets. In the CHOP method, EOC data points are clustered in a number of CHOP groups based on operating condition characteristics rather than on time chronology. The method thereby yields a reduction in calculation times similar to those of averaging methods ([14] [15] [16] [17] [18] [19] [20] [21] [22] [23]) while maintaining information on short-term relations and variations between relevant operating parameters, leading to more accurate solutions. Another advantage of the CHOP method is the fact that all initial EOC data are included in the reduced dataset, as opposed to typical time-period approaches ([28] [29] [30] [31] [32] [33]) where EOC datasets are sought represented by a limited number of periods. Furthermore, the CHOP method provides a possibility for including data on long-term energy system development without *de facto* increasing the number of periods, as opposed to several of the previously described methods ([17] [18] [19] [20] [21] [22]

[23], [28] [29], [34] [35] [36]). The work builds upon a preliminary study presented by Lythcke-Jørgensen et al. [27].

In this paper, the structure and contents of the CHOP method are described in detail in Section 2, where an example is given to demonstrate the use of the method. In Section 3, a simple operation optimization model of a CHP plant is developed, and the model is solved using various reduced EOC datasets to compare the performance of the CHOP method to other common methods. Furthermore, a posteriori error analysis is applied to assess the quality of the results obtained. In section 4 advantages and drawbacks of the CHOP method are discussed and a conclusion of the study is given in Section 5. Various reduced EOC datasets are provided in the Appendix.

2. The Characteristic Operating Pattern method

The Characteristic Operating Pattern (CHOP) method is an original graphic-based data aggregation method for reducing external operating condition (EOC) datasets. The method assumes quasi-static operation and is applicable on datasets in the form of operating points O_j , with each point being characterised by a time of occurrence T_j , a duration t_j^1 , and a number of operating condition parameters \bar{p}_j .

$$O_j = \{T_j, t_j, \bar{p}_j\} \quad (1)$$

In the CHOP method, EOC data points are clustered in groups based on data characteristics rather than the time of occurrence, as opposed to time-chronological averaging methods [[14] [15] [16] [17] [18] [19] [20] [21] [22] [23]]. The clustered groups, called CHOP groups, are introduced as weighted periods in multi-period optimization models. A principal sketch of the data aggregation principle applied in the CHOP method is presented in Figure 1. Dynamics cannot be considered in operation optimization models applying CHOP-reduced datasets as information on time chronology is lost.

Two overall procedures are associated with the CHOP method: The CHOP data aggregation method, and error analysis. The CHOP data aggregation method, which is the core of the method, consists of three principal steps:

¹ $t_{O_j} = 1h$ is commonly used when working with power markets [37], but other values of t_j may be used as well.

1. *Entity selection*: Identification of relevant EOC parameters
2. *Clustering criteria*: Definition of characteristic parameter intervals
3. *Cluster procedure*: Establishment of CHOP groups

As it is desirable to estimate the quality of the results obtained using the reduced dataset, error analysis is an integral part of the CHOP method. Within the framework presented here, one *a priori* and two *a posteriori* analyses are suggested, but others may be relevant as well.

1. *A priori*: Evaluate the standard deviation of parameters in CHOP groups
2. *A posteriori*: Evaluate the quality of the applied datapoint clustering. Analyse the errors made by neglecting dynamic constraints.

Both *a priori* and *a posteriori* error analyses may yield results necessitating reconfiguration of the data aggregation analysis. The overall CHOP method procedure is illustrated in Figure 2.

Next, the contents of the CHOP data aggregation analysis and suggestions for error analyses are presented.

The method is illustrated by an *example*, in which a historical 5-year EOC dataset for a fictive local extraction-based combined heat and power (CHP) plant located in West Denmark is reduced using the method. A principal sketch of the CHP plant is shown in Figure 3.

2.1. CHOP data aggregation method

2.1.1. Entity selection

The first step in the CHOP data aggregation analysis is to select data entities for clustering. This implies 1) identification of EOC parameters p_k for the plant of interest, and 2) assessment of parameter variation:

- 1) **Identification of relevant EOC Parameters**: Within the CHOP method framework, EOCs are defined as boundary conditions that may influence, but are hardly influenced by, operation decisions on plant level, and are therefore regarded as fixed parameters. Any parameter fitting these criteria must be included as an EOC parameter.
- 2) **Parameter variation assessment**: For all identified EOC parameters, the maximum, minimum and mean parameter values over the selected period must be identified based on the reference

datasets. As it is desirable to reduce the number of EOC parameters to define clustering from in order to keep computational effort low, it is recommended that clustering criteria are only defined for EOC parameters with variations higher than $\pm 10\%$ of the period mean value. The potential error from neglecting variations in specific EOC parameters must be assessed as a part of the *posteriori* error analysis, see section 2.2.2.

Example: As illustrated in Figure 3, the CHP plant of interest imports fuel, air, and cooling water, while it produces district heating, power, exhaust gases and heated cooling water.

1) Identification of the relevant EOC parameters

The assumed objective of the CHP plant owner is to obtain the most profitable production. Being the sole heat producer in the district heating system, the production of a CHP plant is constrained by the heating demand. Assuming that cooling is freely available from a cold reservoir, air is freely available from the surroundings, and neglecting taxes on emissions, three relevant EOC parameters exist: Fuel price (coal), heating demand, and power price. Being a single plant located in the well-integrated West Denmark power grid, the power and coal prices can be considered unaffected by the production of the CHP plant. Assuming no demand flexibility on the consumer side, the heat demand is also unaffected by operation decisions. Hence, these three external parameters can be considered as EOC parameters in the CHOP method. This would not have been the case had the CHP plant been the main power producer in an isolated power grid, or if the CHP plant was fuelled by a local distributed biomass like straw [38], in which case the power and/or fuel prices would have been significantly influenced by plant operation decisions.

2) Assessment of parameter variation

Historical parameter datasets over the period 2010-01-01 – 2014-12-31 are considered for the three EOC parameters.

According to data on coal prices from Key World Energy Statistics 2014 provided by the International Energy Agency [39], the yearly average coal price in Denmark's neighbouring country Poland was 80.75 USD/ton over the years 2010-2013, with a maximum price of 84 USD/ton and a minimum price of 78

USD/ton. Assuming that the coal price fluctuations in Poland are analogue to those in Denmark, the resulting variation range is -3.4% to +4% which is well below the recommended clustering threshold of $\pm 10\%$. Therefore, the coal price is not considered as a varying EOC parameter for clustering in the case treated. The error of this assumption will be assessed as a part of the *posteriori* error analysis in Section 3.4. In the given case, the coal price is set to 15.70 Euro/MWh, which is the perceived coal price for 2012 reported by the Danish CHP owner DONG Energy [40].

Data on hourly power prices in West Denmark over the entire period has been extracted from the webpage of the Danish transmission system operator Energinet.dk. [41]. The average hourly power price was 40.08 Euro/MWh, with a maximum price of 2000.00 Euro/MWh and a minimum price of -200.00 Euro/MWh. As this variation is well above the recommended threshold of $\pm 10\%$ of the mean, power price is included as a varying EOC parameter for clustering.

Data on hourly relative heat demand in a Danish district heating system over a year has been extracted from the energy system model STREAM [42]. It is assumed that the annual relative heat demand pattern is repeated for each of the 5 years investigated. The average hourly relative heat demand over the period was 0.55, with a maximum of 1.00 and a minimum of 0.06. As this gives in a variation of -89% to +82% which is well above the recommended threshold of $\pm 10\%$ of the mean, relative heat demand is included as a varying EOC parameter for clustering.

2.1.2. Clustering criteria

Having identified the varying EOC parameters p_k , the second step of the CHOP data aggregation analysis is to define the clustering criteria for aggregating operating points. This is done by splitting the value range of each p_k into a number of characteristic intervals, n_{p_k} . Being empirical in essence, the following graphic-based two-step approach is suggested for breaking up a parameter value range into characteristic intervals based on the cumulative parameter curve. The process is illustrated in Figure 4 with power price as the relevant EOC parameter.

a) **Important values:** Some parameter values may be of special interest, making it relevant to introduce a break at these points. For the power price example, it may be relevant to introduce a break at a power price of 0.00 Euro/MWh to make sure that negative prices are grouped together. Also, if an operating decision, e.g. turning on a piece of equipment, is dependent on a given power price, an interval break should be introduced at this price as well. It is also suggested that if significant trend changes occur in the cumulative curve, the parameter values of points separating various trends should be included as important values.

b) **Even division:** If the already set break-points are far from each other in terms of both parameter value and duration, it is suggested that additional interval breaks are introduced to minimize the span. The break-points should be located so that the parameter value range is constant for each of the intervals.

It is essential that all feasible parameter values are covered within the characteristic parameter intervals. It may be necessary to define the first and last of the characteristic intervals as open. The necessary number of intervals for each parameter depends on the parameter value volatility, the significance of the parameter and the data available. In Figure 4, six intervals were defined in the visual power price example, while it may be sufficient to define just two or three intervals for less volatile parameters. In contrast, more intervals may be defined for the power price in case it has significant impact on the optimization model. It should be noticed that if only one characteristic interval is defined for a parameter, it will be included as a constant in the final CHOP-reduced dataset.

Example: The cumulative curve for power prices, also known as the power price duration curve, is obtained by sorting the data points according to the value of the power price value. The cumulative curve illustrates the aggregated duration of power prices over the period, and is shown in Figure 5.

Using the suggested two-step approach for breaking up the cumulative curve for power prices, the following break points are obtained:

a) Important values: 0.00, 25.00, 65.00 [Euro/MWh]

270 b) Even division: 35.00, 45.00, 55.00 [Euro/MWh]

271 This leads to seven characteristic intervals for the power price, which are summarized in Table 1.

272 The cumulative curve for the relative heat demand, which illustrates the aggregated duration of relative
273 heat loads over the period, is shown in Figure 6.

274 Using the suggested two-step approach for breaking up the cumulative curve for relative heat demand, the
275 following break points are obtained:

276 a) Important values: 0.25, 0.65, 0.95^b [-]

277 b) Even division: 0.125, 0.45, 0.80 [-]

278 ^b It is relevant to group peak heat-demand operating points together for heat production dimensioning purposes.

279 This leads to seven characteristic intervals for the relative heat demand, which are summarized in Table 2.

280 2.1.3. Cluster procedure

281 The final part of the data aggregation analysis is the cluster procedure, which involves the definition of
282 CHOP groups and clustering and aggregation of data points in the CHOP groups.

283 By definition, any combination of characteristic parameter intervals is a potential CHOP group. Hence, the
284 number of potential CHOP groups in a dataset, $N_{CHOP,pot}$, is determined by the number of characteristic
285 parameter intervals n_{p_k} defined for each of the varying EOC parameters p_k :

$$286 \quad N_{CHOP,pot} = \prod_{p_k} n_{p_k} \quad (2)$$

287 To maintain an overview, it is suggested that the potential CHOP groups are indexed using the following
288 key:

$$289 \quad G_l = G(i_{p_1}, i_{p_2}, \dots, i_{p_k}) \quad (3)$$

290 Here, G is short for group, and $i_{p_n} \in \{1, \dots, n_{p_k}\}$ is the interval number i of the varying EOC parameter p_k .

291 For example, if two varying EOC parameters are defined in a CHOP-reduced dataset, the CHOP group

292 $G(2,5)$ represents the combination of ' p_1 interval 2' and ' p_2 interval 5'. EOC parameters considered as

293 constants are not included in the indexing key.

294 All data points O_j of the initial dataset are sorted into the potential CHOP groups G_l based on their EOC
 295 parameter values. Each CHOP group G_l becomes an operating point in the final dataset characterised by a
 296 duration t_l (the sum of durations of the aggregated data points), and a number of operating condition
 297 parameters \bar{p}_l (the weighted average parameter values of the aggregated data points).

$$298 \quad G(i_{p_1}, i_{p_2}, \dots, i_{p_k}) = G_l = \{t_l, \bar{p}_l\} \quad (4)$$

$$299 \quad t_l = \sum_{O_j \in G_l} t_j \quad (5)$$

$$300 \quad \bar{p}_l = \frac{\sum_{O_j \in G_l} \bar{p}_j \cdot t_j}{t_l} \quad (6)$$

301 It should be noted that the vector \bar{p}_l includes all EOC parameters, but it may also include other external
 302 parameters that are unaffected by the plant operation. It is evident that the duration t_j represents the
 303 weight given to a given operating point O_j in the CHOP dataset. In case the time-value of money is
 304 considered in the optimization model, t_j can be represented in the form of present value factor $t_{PV,j}$ as
 305 well.

306 If no data points belong to a potential CHOP group, the group is excluded from the final CHOP dataset.

307 Hence, the final number of CHOP groups is lower than or equal to the number of potential CHOP groups:

$$308 \quad N_{CHOP} \leq N_{CHOP,pot} = \prod_{p_k} n_{p_k} \quad (7)$$

309 The defined CHOP groups G_l replace the initial dataset of operating points in an optimization model,
 310 thereby reducing the number of periods to be considered.

311 *Example:* Three EOC parameters are considered: Relative heat demand p_1 , power price p_2 , and coal price
 312 p_3 . The number of characteristic parameter intervals are $n_{p_1} = 7$, $n_{p_2} = 7$, and $n_{p_3} = 1$. Hence, the
 313 number of potential CHOP groups $N_{CHOP,pot}$ is

$$314 \quad N_{CHOP,pot} = \prod_{p_k} n_{p_k} = 49 \quad (8)$$

315 Based on the reference dataset, a simple algorithm written in Excel was applied for sorting reference data
 316 points into CHOP groups. Using equations (4)-(6), the algorithm further calculated durations and parameter
 317 values for the identified CHOP groups. The processing of the entire dataset took approximately 30 seconds

318 using a laptop with an Intel® Core™ i7-3720QM CPU with 2.60 GHz and 8 GB RAM. The calculated values
319 are summarized in Table 3.

320 The number of CHOP groups is found to be

$$321 \quad N_{CHOP} = 46 < N_{CHOP,pot} \quad (9)$$

322 as no data points belongs to the potential CHOP groups $G(1,1)$, $G(1,7)$ and $G(7,1)$. An illustration of the
323 sorting of data points into CHOP groups and the resulting CHOP groups is presented in Figure 7.

324 2.2. Error analysis

325 2.2.1. A priori

326 Having conducted the data aggregation analysis, it is possible *a priori* to calculate the standard deviation
327 $\sigma_{p_{k,l}}$ for each parameter p_k in a CHOP group G_l .

$$328 \quad \sigma_{p_{k,l}} = \sqrt{\frac{1}{t_l} \sum_j \left(t_j (p_{k,j} - p_{k,l})^2 \right)} \quad (10)$$

329 with t_j being the duration of an operating point $O_j \in G_l$ and t_l being the summarized duration of G_l . The
330 standard deviation may give an impression of the scatter of the merged operating points within each CHOP
331 group and thereby estimate the accuracy error of aggregating numbers in the defined CHOP groups. If the
332 standard deviation of a parameter is significantly larger in one CHOP group than in the others, the cause of
333 the deviation should be investigated. Significant standard deviations may indicate that additional
334 characteristic intervals have to be defined in the CHOP data aggregation analysis.

335 *Example:* The standard deviation is calculated for the relative heat demand and power price of the CHOP
336 groups defined in Table 3. The results are presented in Table 4 and Table 5.

337 Concerning the standard deviation of the relative heat demand, it is seen that the largest deviations occur
338 for the heat intervals 3 and 4, owing to the fact that these two intervals are the ones with the largest value
339 span. The standard deviations are not found to vary significantly, and it is therefore not considered
340 necessary to change the characteristic intervals for the relative heat demand.

341 Regarding the standard deviation of the power price, significant differences are obtained for power price
342 intervals 1 and 7. The reason is that the intervals contain extreme parameter values as they are open
343 towards the infinite. Especially groups $G(5,1)$ and $G(4,7)$ show large standard deviations, which is also
344 evident from Figure 7. For $G(5,1)$, the major deviation is caused by 8 hours on the December 25th 2012
345 when the average power price was -174.87 Euro/MWh. For $G(4,7)$, the main cause of the large deviation is
346 5 hours on June 7th 2013 when the average power price was 1940.82 Euro/MWh. Based on these findings, it
347 is not deemed relevant to change the characteristic intervals *a priori*.

348 2.2.2. A posteriori error analysis

349 Having solved an optimization model using CHOP-reduced datasets, two suggestions for *a posteriori*
350 analyses are presented here: A sensitivity analysis for verifying the quality of the CHOP-groups and
351 selection of varying EOC parameters, and an error analysis for estimating errors from neglecting time
352 chronology-dependent constraints, such as production ramp rates or thermal storages.

353 To verify the quality of the CHOP-group clustering criteria, new CHOP datasets can be defined from the
354 initial EOC dataset but with additional characteristic intervals for each parameter. New operation
355 optimization runs can then be made for selected designs using the new CHOP group datasets. If results of
356 the various runs differ significantly, it may suggest that the characteristic intervals have been defined too
357 loosely and that a more detailed CHOP data aggregation should be conducted for the dataset.

358 *Example:* An example of how to evaluate the CHOP group clustering criteria using sensitivity analysis, and
359 to assess the expected error of including an EOC parameter as a constant, is given in Section 3.4.

360 Some optimization models may include constraints that require knowledge on time chronology, for
361 instance ramp-rate or thermal storage constraints. However, this information is not sustained in CHOP-
362 reduced datasets. If an optimization model with time chronology-dependent constraints is run using CHOP-
363 reduced EOC datasets, the error of neglecting these constraints must be assessed *a posteriori*. This can be
364 done by first solving the optimization model using the CHOP-reduced EOC dataset. The found optimal

operation pattern can then be applied on the initial EOC dataset, and the resulting error of neglecting the constraint can be calculated.

Example: An example of how to assess the error of including a thermal storage in an optimization model using a CHOP-reduced EOC dataset is presented in Section 3.5.

3. Illustrative case: Operation optimization of a Danish extraction-based combined heat and power plant

In this section, the advantage of applying the CHOP method is illustrated by extending the CHP-example of section 2. Here, the operation of the fictive Danish extraction-based CHP is optimized over the 5-year period 2010-01-01 – 2014-12-31. The optimization is carried out using the entire EOC dataset, the CHOP-reduced dataset, a yearly averaged dataset, a monthly averaged dataset, and a seasonal peak/off-peak averaged dataset. The results obtained are compared with respect to problem size and accuracy.

3.1. Optimization model

A linearized model of the existing Danish extraction-based CHP plant Avedøreværket 1 (AVV1) is developed to represent the fictive Danish CHP plant treated in the example. AVV1 was commissioned in 1990 and has a net power production of 250 MW in condensation mode and 212 MW in full back pressure mode with a district heating production of 330 MJ/s (drive temperature/return temperature 100°C/50°C) [43]. Part-load operation in the CHP unit is governed by sliding-pressure control [44]. The minimum load λ_{min} considered of AVV1 is $\lambda_{min} = 0.4$.

A thermodynamic model of AVV1 was previously developed by Elmegaard and Houbak [43] using the energy system simulator Dynamic Network Analysis [45]. The model was validated by Lythcke-Jørgensen et al. [25], who found that the model-predicted electrical efficiency in condensation mode was 2%-8% lower than that reported by the plant owner, but that the model in general was accurate with respect to electrical and first-law energy efficiency. The linearized model developed here is based on the model by Elmegaard and Houbak [43].

389 The linearized model is based on two assumptions: The power-to-heat production ratio C_v is constant, and
 390 the fuel-consumption is a linear function of the load. Four central operating points in the reference model
 391 {A, B, C, D} are used for developing the linearized model: A is operation in full-load condensation-mode, B is
 392 operation in minimum-load condensation-mode, C is operation in full-load back-pressure-mode, and D is
 393 operation in minimum-load back-pressure-mode.

394 In the linear model, the linearized operating points A^* and C^* are set equal to the reference points A and C,
 395 while heat production in the linearized points B^* and D^* is set equal to the heat production of reference
 396 points B and D.

$$397 \quad A^* = A, \quad C^* = C, \quad Q_B^* = Q_B, \quad Q_D^* = Q_D \quad (11)$$

398 The linearized power-to-heat ratio C_v^* is defined as the average of the overall heat-to-power ratios at
 399 maximum load, $C_{v,\lambda_{max}}$, and minimum load $C_{v,\lambda_{min}}$:

$$400 \quad C_{v,\lambda_{max}} = \frac{Q_B}{P_A - P_B} \quad (12)$$

$$401 \quad C_{v,\lambda_{min}} = \frac{Q_D}{P_C - P_D} \quad (13)$$

$$402 \quad C_v^* = \frac{C_{v,\lambda_{max}} + C_{v,\lambda_{min}}}{2} = 9.406 \quad (14)$$

403 The power production in the linearized points B^* and D^* are found using equations (11) and (14). Data on
 404 the four reference points {A, B, C, D} and the corresponding linearized points { A^* , B^* , C^* , D^* } are presented
 405 in Table 6.

406 For any heat production Q , the maximum power production in the linearized model P_{max}^* , which
 407 corresponds to a power production at a load $\lambda = 1.0$, is

$$408 \quad P_{max}^* = P_A^* - \frac{Q}{C_v^*} \quad (15)$$

409 Two constraints exist on the minimum power production in the linearized model, P_{min1}^* and $P_{min2}^* \cdot P_{min1}^*$
 410 is the minimum feasible power production as a consequence of the minimum load constraint $\lambda_{min} = 0.4$,
 411 while P_{min2}^* is the minimum feasible power production as a consequence of the back-pressure operation-
 412 mode constraint $\alpha_{max} = 1.0$. Both of these constraints must be satisfied.

$$P_{min1}^* = P_C^* - \frac{Q}{C_v^*} \quad (16)$$

$$P_{min2} = P_D^* + (Q - Q_D^*) \frac{P_B^* - P_D^*}{Q_B^* - Q_D^*} \quad (17)$$

The feasible power-heat operation area of the linearized model is defined by the constraints (15)-(17). The power-heat operation area of the reference model, the linearized model, and the four reference operating points {A, B, C, D} are shown in Figure 8.

Evaluating the accuracy of the linear approximated equations (15)-(17), it is found that the accuracy on the power constraints is within -1.45% to 2.69%. The largest negative deviation occurs for the maximum power production at $Q = 194.5 \text{ MJ/s}$, and the largest positive deviation occurs for the minimum power production at $Q = 118.6 \text{ MJ/s}$.

In the linearized model, the load can be calculated as a function of the heat and power production:

$$\lambda(P, Q) = \lambda_{min} + (1 - \lambda_{min}) \frac{\left(P + \frac{Q}{C_v^*}\right) - P_C^*}{P_A^* - P_C^*} \quad (18)$$

The linearized fuel consumption $F^*(\lambda)$ in MJ/s as a function of the load is found using the first-order trendline function in Microsoft Excel on data for fuel consumption at various loads in the AVV1 model.

$$F^*(\lambda) = F^*(P, Q) = 499.64 \cdot \lambda(P, Q) + 102.179 \quad (19)$$

A coefficient of determination of $R^2 = 0.9998$ was obtained for this trendline function.

The operation of the fictive Danish CHP plant is to be optimized with the aim of minimizing the costs of producing heat to the district heating network over the period 2010-01-01 – 2014-12-31. The variables of the optimization model are the power production P_j and heat production Q_j in each period j . As discussed in Section 2.1., the CHP production is constrained by the heating demand which has to be met at all times.

To simplify matters, thermal energy storage is neglected, hence Q_j is constrained by

$$Q_j = Q_{j,ref} \quad \forall j \quad (20)$$

The power production P_j is constrained by equations (15)-(17). *Full hour-wise operation flexibility is assumed for the plant, and, consequently, the choice of (P_{j+1}, Q_{j+1}) is independent of (P_j, Q_j) .*

Assuming that operation and maintenance costs are constant and therefore indifferent to the choice of (Q_j, P_j) , that air is free and cooling is freely available from a cold reservoir, and neglecting taxes on emissions, the objective function to be minimized can be defined as

$$C_{heat}(Q_j, P_j) = \sum_j [F^*(P_j, Q_j) \cdot c_{fuel,j} - P_j \cdot c_{p,j}] \quad (21)$$

Here, $C_{heat}(Q_j, P_j)$ is the variable cost of the heat production, $c_{fuel,j}$ is the cost of fuel, and $c_{p,j}$ is the power price in each operating point j .

Given equations (15)-(21), the optimization problem can be written in condensed form as

$$\begin{cases} \min_{Q,P} [C_{heat}(Q_j, P_j)] \\ \text{subject to constraints:} \\ \text{equations (15), (16), (17), (20)} \\ \text{with variables:} \\ P_j, Q_j \in \mathbb{R}^+ \end{cases} \quad (22)$$

3.2. External operating conditions datasets

Five different EOC datasets are used for solving optimization problem (22): The full EOC dataset, which is obtained by combining data on hourly power prices in the West Denmark power grid [41] with data on hourly relative heat demand for Denmark [42], as discussed in Section 2.1.2; the CHOP-reduced EOC dataset D_{CHOP} , which is presented in Table 3; the annually averaged EOC dataset D_{AA} , in which the EOC parameter values are averaged over each of the five years; the monthly averaged EOC dataset D_{MA} , in which the EOC parameter values are averaged over each of the 60 months in the period; and, finally, the seasonal peak/off-peak averaged EOC dataset D_{SP} , which is inspired by the approach taken by Chen et al. [2] for representing EOC parameters. Here, EOC parameter values are averaged over the peak period, 7 a.m.-11 p.m., and off-peak period, 11 p.m.-7 a.m., for each of the four seasons each year. Datasets D_{AA} , D_{MA} , and D_{SP} are presented in the Appendix. A scatter diagram illustrating the reference EOC dataset and the reduced datasets is presented in Figure 9.

Figure 9 illustrates how the parameter value diversity of the reference dataset is sustained in the various reduced datasets. It is seen that the annual average EOC dataset yields five points, all located in the centre of Figure 9, that are almost identical with respect to relative heat demand and power price. The monthly

459 averaged and seasonal peak/off-peak averaged EOC datasets are seen to be more distributed, but the
460 resulting operating points are still far from the borders of the dense cloud of reference operating points.
461 Opposed to this, both the CHOP and the CHOP-revised EOC datasets are seen to be significantly more
462 distributed in the figure, suggesting that a larger degree of the diversity in the reference dataset is
463 sustained in these reduced datasets.

464 3.3. Results and comparison

465 The optimization problem (21) is solved using the open-source mixed-integer program solver CBC (COIN
466 Branch and Cut) [46] in OpenSolver 2.6.1 [47] for Microsoft Excel. The optimization results obtained using
467 each of the five EOC datasets are summarized in Table 7.

468 Firstly, it is evident that by optimizing the operation of the CHP unit using the full dataset it is possible to
469 reduce the total variable heat cost to $C_{heat} = 0.38$ MEuro. This value is the exact solution to the
470 optimization problem (21) under the given conditions and assumptions, and the results obtained using the
471 full dataset are used as reference values for further comparison.

472 Among the reduced EOC datasets, the result obtained using D_{CHOP} gets closest to the reference value with
473 a deviation of 0.38 MEuro in total variable heat cost. Compared to this, the deviation is 8.15 MEuro when
474 using D_{AA} , 7.64 MEuro using D_{MA} , and 5.58 MEuro using D_{SP} . In terms of computation time, the number of
475 calculations to be performed is 5 when using D_{AA} , 60 when using D_{MA} , 40 when using D_{SP} , and 46 when
476 using D_{CHOP} . Hence, D_{CHOP} obtains the most accurate economic result of the reduced datasets for the case,
477 while the relative reduction in computation time from using D_{CHOP} is comparable to those of using D_{MA}
478 and D_{SP} . This demonstrates the relevance of the CHOP method for reducing datasets on external operating
479 conditions.

480 For the results obtained using D_{AA} , D_{MA} and D_{SP} , it is seen that the total power production and fuel
481 consumption are larger than the reference values. This is caused by the fact that the operation optimization
482 only considers the average power prices of the periods. Hence, if the average power price over a given
483 period is economically attractive for power production at the plant, power production is maximized over

the entire period even though the power price may not be attractive in all hours. This phenomenon results in an increased power production, but also in increased fuel costs that exceed the increased income from power sales and yielding a higher C_{heat} for the three solutions compared to the reference solution. The opposite trend, where power production is minimized for entire periods containing data points with advantageous power prices, also occurs when using D_{AA} , D_{MA} and D_{SP} , but the first trend is found to be dominant in the present case.

In contrast, the result obtained using the D_{CHOP} dataset underestimates the power production in the case investigated, and also shows reduced income from power sales. At the same time an almost equal reduction in fuel costs occurs, resulting in the relatively low deviation in the heat price compared to the reference result. The explanation is that in the CHOP method, the data points merged in CHOP groups have similar parameter values. Hence, averaged parameter values are close to the parameter values of the data points. If the power is minimized over a data point where it would be maximized in the reference case, or vice versa, the economic difference is small. Thus, when using the D_{CHOP} dataset, the economic result is very close to that of the reference optimization.

Comparing the accuracy of results, it is seen that the estimated fuel consumption and power production are overestimated by 2.5% and 3.4% using D_{AA} , by 4.4% and 5.7% using D_{MA} , by 2.2% and 2.8% using D_{SP} , while they are underestimated by 3.1% and 4.1% using D_{CHOP} . This indicates that the optimal operation pattern predicted using D_{CHOP} is different from the reference optimum for a significant amount of operating points for the given case, suggesting that the CHOP clustering criteria could be improved. This had not been obvious if the reference solution had not been known, or if only the economic objective had been considered. Therefore, it is suggested that sensitivity analysis is applied *a posteriori* for evaluating the quality of the applied clustering criteria, and thereby assessing the accuracy of the results.

3.4. Sensitivity analysis

A posteriori, sensitivity analyses are conducted to evaluate the quality of the entity selection and the applied clustering criteria.

509 First, the impact of not including coal price as a varying EOC parameter in the CHOP analysis is assessed. As
510 described in Section 2.1.1., the data suggested that the coal price varied within the range -3.4% to +4% of
511 the average price over the period. It is here assessed how such variations would affect the optimized
512 operating pattern when using the CHOP dataset.

513 In the optimization model, the heat production is constrained and therefore unaffected by the coal price.
514 However, power production is flexible and depends on power prices and coal prices. The impact on power
515 production and fuel consumption from varying the coal price within the range $\pm 5\%$ over the entire period
516 is shown in Figure 10. It is seen that if the coal price is reduced by 5%, the power production is increased by
517 1.2% and the fuel consumption by 0.9%. Apart from this, the power production and fuel consumption are
518 hardly affected by variations in the coal price over the set range. It is therefore considered acceptable to
519 use the average coal price value in the CHOP dataset.

520 Next, the applied clustering criteria are assessed. Here, the number of characteristic intervals defined for
521 the relative heat demand and power price is varied and new CHOP datasets are obtained. The optimization
522 model is then run using each of the new CHOP datasets to evaluate the impact on the results of changing
523 the clustering criteria.

524 Three sensitivity analyses are considered: Heat interval sensitivity, where the number of intervals defined
525 for the relative heat demand is changed; power interval sensitivity, where the number of intervals defined
526 for the power price is changed; and combined heat and power interval sensitivity, where the number of
527 intervals defined for both the relative heat demand and the power price are changed simultaneously. The
528 interval break points defined for the sensitivity analyses are given in Table 8.

529 The results obtained by running the optimization model with the modified CHOP datasets are compared
530 with respect to income result, fuel cost, power production and power sales. The outcomes are presented in
531 Figures 11-14.

532 Figure 11 shows the variations in total variable heat cost from the different sensitivity analyses. It is seen
533 that *reducing the number of power intervals with the suggested break-points significantly increases the*

534 *total variable heat cost*, while increasing the number of intervals leads to slightly better results. A stable
535 level is reached when increasing the number of power price intervals to 8-10 with the set break points. This
536 suggests that the number of characteristic intervals for the power price should be increased in order to
537 obtain a robust solution. Opposed to this, *the result is almost unaffected by the number of relative heat*
538 *demand intervals defined*, suggesting that the initial resolution of 7 characteristic heat demand intervals is
539 sufficient. Both findings are supported by the combined heat and power intervals sensitivity analysis, the
540 trend of which is almost identical to that of the power interval sensitivity.

541 Furthermore, the findings above are supported by the analogue results obtained when comparing the
542 sensitivity analysis results with respect to fuel costs (Figure 12), power production (Figure 13), and power
543 sales (Figure 14). Again, it is found that the results are somewhat unaffected by minor changes in the
544 number of relative heat demand characteristic intervals, while the results obtained become stable when
545 the number of power price intervals is increased to 8 or more using the suggested interval break-points.

546 The sensitivity analysis suggests that the CHOP dataset should be reconfigured by changing the number of
547 characteristic power price intervals to 8 using the interval break-points presented in Table 8. The revised
548 CHOP dataset is presented in Table 9, while results obtained using the revised CHOP dataset are presented
549 in Table 10. The results show that the C_{heat} obtained is practically identical to that found using the
550 reference data when applying the revised CHOP dataset, while the power production and fuel consumption
551 are underestimated by less than 1%, suggesting that the revised clustering criteria is more accurate than
552 the initial one. In terms of reduction in relative computation time, the revised CHOP dataset requires 53
553 calculations, a number which is comparable to the number of calculations required when using D_{MA} and
554 D_{SP} as well.

555 3.5. Optimization with thermal energy storage

556 As discussed by Rolfsman [48], the income from power sales in CHP plants may be increased by installing
557 thermal energy storages that allows for production shifting in periods with high power prices. Similar
558 results were reported by Martínéz-Lear et al. [49] for combined heating, cooling and power plants for

559 buildings. Hence, optimization models of multi-generation plants dealing with heating or cooling
 560 production should preferably include an option for thermal storage. In this section, the optimization model
 561 (22) is rewritten to include short-term heat storage, and the error made from solving the problem using the
 562 revised CHOP dataset (Table 9) is assessed.

563 In the case of the fictive Danish CHP plant, it is assumed that a thermal energy storage capable of storing 24
 564 hours of peak heat production is available on site.

$$565 \quad Q_{storage,max} = 24 \cdot 332.91 MWh = 7990 MWh \quad (23)$$

566 Heat losses are neglected in the thermal energy storage model. The thermal energy storage content

567 $Q_{storage,j}$ is calculated as

$$568 \quad Q_{storage,j} = Q_{storage,j-1} + (Q_j - Q_{j,ref}) \quad , \quad Q_{storage,0} = 0 \quad (24)$$

569 In the rewritten optimization problem, the constraint (19) is slacked and replaced by a new constraint

570 stating that the total heat production over the entire period must equal the total heat consumption

$$571 \quad \sum_j Q_j = \sum_j Q_{j,ref} \quad (25)$$

572 Furthermore, two constraints are introduced representing the physical constraints of the thermal energy

573 storage:

$$574 \quad Q_{storage,j} \leq Q_{storage,max} \quad (26)$$

$$575 \quad Q_{storage,j} \geq 0 \quad (27)$$

576 Given equations (15)-(19) and (23)-(27), the optimization problem with thermal energy storage can be

577 written in condensed form as

$$578 \quad \begin{cases} \min_{Q,P} [C_{heat}(Q_j, P_j)] \\ \text{subject to constraints:} \\ \text{equations (15), (16), (17), (25), (26), (27)} \\ \text{with variables:} \\ P_j, Q_j \in \mathbb{R}^+ \end{cases} \quad (28)$$

579 As constraints (26) and (27) require knowledge of the time chronology of the data points, the optimization

580 problem (28) cannot be solved using the CHOP-reduced dataset. Therefore, constraints (26) and (27) were

581 slacked, and the resulting error was evaluated a posteriori. Results obtained from solving the problem (28)
582 using the full EOC dataset and the revised CHOP dataset are presented in Table 11.

583 When solving problem (28) using the full EOC dataset, a total variable heat cost of -6.08 MEuro was
584 obtained, as opposed to the solution where no heat storage was considered and a total variable heat cost
585 of 0.38 MEuro was obtained. The negative costs means that power sales exceed the total fuel costs in
586 optimal operation for the CHP plant. The result suggests that short-term thermal energy storage is an
587 economic advantage in CHP production, supporting the outcomes presented by Rolfsman [48] and
588 Martínéz-Lear et al. [49]. It is further seen that the power production is slightly reduced while incomes from
589 power sales are increased when comparing to the situation without heat storage. This is owing to the fact
590 that heat storage allows for a more flexible production.

591 Solving problem (28) with the revised CHOP dataset gives a total variable heat cost of -8.06 MEuro. It is
592 seen that the power production, power sales, and fuel consumption are all reduced when compared to the
593 solution obtained using the full EOC dataset. The economic result is slightly improved when compared to
594 the result obtained using the full EOC dataset. However, the results cannot be directly compared without
595 assessing the error that slacking of constraints (26) and (27) imposes on the CHOP solution.

596 By applying the optimal operation pattern predicted by the CHOP solution on the chronological EOC
597 dataset, it is possible to evaluate the contents of the thermal energy storage over the 5-year period
598 investigated. A plot of the thermal energy storage contents over the 5-year period for the optimal solutions
599 to problem (28) obtained using the full EOC dataset and the revised CHOP dataset is presented in Figure 15.

600 It is seen that the CHOP solution significantly violates the physical constraints of the thermal energy storage
601 in the model over the 5-year period. The explanation is quite simple: When slacking constraints (26) and
602 (27), the only constraint on the heat production is that heat production and consumption must be balanced
603 over the entire period. As the power prices on average were higher in the first two years of the period
604 (consult Table 12 in the Appendix), power production is maximized at the cost of heat production in 2010
605 and 2011, while excess heat is produced the following years when power prices are lower. It can also be

deducted from the graph that additional heat is produced in the summer periods when demand is low, and then stored for use in the winter when heat demand is high. Though highly intuitive, this solution is infeasible in reality due to thermal energy storage constraints. The results illustrates that the CHOP method may not be suitable for data reduction in models where short-term thermal energy storage is considered.

4. Discussion and perspective

As the optimization of FMG concepts is complex and involves such challenges as synthesising and dimensioning of processes, process integration, and operation optimization, it is desirable to reduce external operating condition (EOC) datasets to be used in multi-period optimization models in order to make the models solvable. The CHOP method presented in this paper is a simple method for reducing EOC datasets by clustering data points in groups. The main advantages of the CHOP method include the significant reduction in the size of input data to multi-period optimization problems and the consequent reduction in computation costs, the simple and straight-forward use, and the fact that short-term relations and variations between various operating conditions are sustained in CHOP-reduced dataset. For the simple case study presented in this paper, which treated the operation optimization of a fictive Danish CHP plant, it was found that the solution obtained using the revised CHOP-reduced EOC dataset had a much higher accuracy in terms of economic result and estimations of power production and fuel consumption than the solutions obtained using chronology-averaged EOC datasets. Furthermore, it was found that the revised CHOP dataset reduced the relative amount of computations by approximately a factor 827, which is comparable to the reductions of approximately a factor 730 when using monthly averaged dataset and approximately a factor 1096 when using the peak/off-peak averaged dataset. For the simple case, the advantage of the reduction in computation costs was not evident as the linear optimization problem could be solved within a minute using the full dataset. However, if more advanced optimization models needed be evaluated, e.g. non-linear operation optimization models, and if these further needed be solved for a large number of different designs for each operating point as in the design optimization of complex FMGs, reductions in computation costs is needed. Hence, the combination of high

631 accuracy and significant reduction in computation time support the proposition that the CHOP method is
632 relevant for reducing EOC datasets to be used in optimization models of FMGs, and that the method is to
633 be preferred over any of the three averaging methods mentioned in this paper.

634 The advantage of sustaining information on short-term parameter relations will assumedly be even more
635 significant in more complex optimization models that consider multiple processes. For instance, if a process
636 was considered for integration in the case study CHP plant which would only be economic advantageous to
637 run when power prices are below 25.00 Euro/MWh, it would never be operated if annual or monthly
638 averaged datasets were applied in the optimization model, while it would be run for 2192 hours over the
639 five year period if the peak/off-peak averaged dataset was used, and for 4550 hours, or more than 10% of
640 the time, if the CHOP-reduced dataset or the reference dataset were applied. Sustained data diversity in
641 CHOP-reduced datasets thus allows for more accurate solutions. The fact that a large part of the initial
642 dataset parameter diversity is sustained in the CHOP-reduced dataset is also evident from Figure 9, which
643 illustrates how the parameter diversity in defined CHOP groups is significantly larger than for any of the
644 three averaged datasets. Furthermore, for equipment with performance that is a non-linear function of an
645 EOC parameter, e.g. the power production of a wind turbine as a function of the wind speed, the use of
646 CHOP-reduced datasets rather than chronological-averaged datasets will assumedly yield more accurate
647 results.

648 Another advantage of the CHOP method is the fact that larger datasets do not necessarily yield larger
649 reduced datasets. In the case study, hourly heat demand and power price data were considered for a 5-
650 year period. The initial 43,824 data points were reduced to 60 data points using the monthly averaging
651 method, 40 data points using the seasonal peak/off-peak averaging method, and 53 using the CHOP
652 method. If the period considered was extended to a 30-year period, the number of data points would be
653 multiplied by six for each of the chronological-averaged methods, while it is likely that the number of
654 CHOP-groups would not need to be changed. Instead, the weight given to each of the CHOP groups defined
655 would increase as the additional data points are sorted into the groups. However, it is likely that the

656 increase in weight will not be the same for all CHOP groups due to the development of the energy system.

657 If the time-value of money needs to be considered, the time weight given to each sorted data point can be

658 replaced by a present value weight factor, as discussed in section 2.1.3., allowing for net present value

659 calculations in design optimization models.

660 Error analysis is central in the CHOP method as it provides the feedback required to optimize the data

661 aggregation strategy. In the present work, a number of approaches for conducting the error analysis were

662 suggested. However, it must be emphasized that other methods may be applied as long as they do not

663 counteract the initial ambition of reducing overall computation time. One example of a method that may

664 be useful for error analysis in the CHOP method is the global sensitivity analysis Morris Screening [50],

665 which could be applied *a posteriori* for assessing the quality of the defined characteristic interval breaks by

666 estimating the aggregated impact of varying EOC parameters within the defined intervals, or to evaluate if

667 a non-clustering EOC parameter ought to be included in the clustering analysis.

668 Two significant draw-backs exist for the CHOP method. Firstly, the number of CHOP groups defined is

669 combinatorial as a function of the relevant EOC parameters defined for a given problem. In the case study,

670 three EOC parameters were considered, of which one was excluded from the clustering analysis, and seven

671 and eight characteristic intervals were defined for the other two, resulting in 56 potential CHOP groups

672 according to equation (2). However, if two additional EOC parameters were considered for clustering with

673 four characteristic intervals each, the number of potential CHOP groups would increase to 896. Even

674 though the final number of CHOP groups may be lower according to equation (7), the combinatorial issue

675 represents a significant challenge when applying the CHOP method on datasets with multiple EOC

676 parameters. This also explains why it is relevant to seek to exclude less volatile parameters from the CHOP

677 data aggregation in the entity selection. One way of circumventing the combinatorial issue is to set up

678 relations for deriving various parameters from a few EOC parameters. For example, it may be possible to

679 derive formulas for heating and cooling demands as a function of the outdoor temperature [51] or the cost

680 of various fuels as a function of the expected oil price [2]. If such relations are introduced, the uncertainty

of the applied relations should be included in the sensitivity and error analyses conducted for results obtained.

Secondly, the CHOP method does not permit consideration of dynamics and time chronology directly, which is also the case for yearly- and monthly-averaged datasets. This implies that ramp constraints on operation cannot be considered, potentially resulting in infeasible operation patterns as discussed by Rong and Lahdelma [52], and that thermal energy storages cannot be directly included, as discussed in section 3.5. Also, scheduling of maintenance shut-downs cannot be considered when using CHOP-reduced datasets, and neither can investment planning if the entire reference dataset is reduced to a single CHOP-reduced dataset. The latter can be solved by setting a time-span for investment planning, e.g. 5 years, and then derive a CHOP-reduced dataset for every 5-year period. However, this would increase the size of the dataset significantly, counteracting one of the initial advantages of the CHOP-method.

To overcome the challenges of including thermal energy storage and ramp constraints, it is suggested that CHOP-reduced datasets, rather than yearly or monthly reduced datasets, are applied in a first-step design optimization run, and that a detailed operation optimization is carried out in a sequential step for the most promising designs, similar to the method presented by Rubio-Maya et al. [22] and Uche et al. [23].

5. Conclusion

This study presents a novel and simple method, the Characteristic Operating Pattern (CHOP) method, for reducing external operating condition (EOC) datasets in optimization models. The method has been tailored for optimization models of flexible multi-generation plants (FMGs), but may be suitable for any optimization model that involves a flexible facility operating on multiple markets.

In a case study, an operation optimization model of a Danish extraction-based combined heat and power plant is solved using the full EOC dataset, a CHOP-reduced EOC dataset, a yearly-averaged EOC dataset, a monthly-averaged EOC dataset, and a seasonal peak/off-peak EOC dataset. The results indicate that the CHOP-reduced dataset yields by far the most accurate solution among all the reduced EOC datasets, while achieving a reduction in the problem size similar to those achieved of using monthly-averaged and seasonal

706 peak/off-peak-averaged datasets. It is found that CHOP-reduced datasets are not suited for models that
707 consider short-term thermal energy storage as time chronology is not considered.
708 The outcomes of the paper suggest that the CHOP method is better suited for reducing EOC datasets in
709 optimization models of FMGs than any of the three chronology-averaged methods used for comparison in
710 this paper. If short-term thermal energy storage or ramp constraints are considered, it is suggested that the
711 CHOP method is applied in a first-step design optimization method, and that detailed operation
712 optimization, including dynamic constraints, is carried out in a sequential step for the most promising
713 designs. The latter will be a topic for future research by our group.

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720 **Appendix**

721 This appendix presents the reduced external operating condition (EOC) datasets D_{AA} (Table 12), D_{MA}
722 (Tables 13-15), and D_{SP} (Tables 16-18) as explained in Section 3.2.

Figure 1

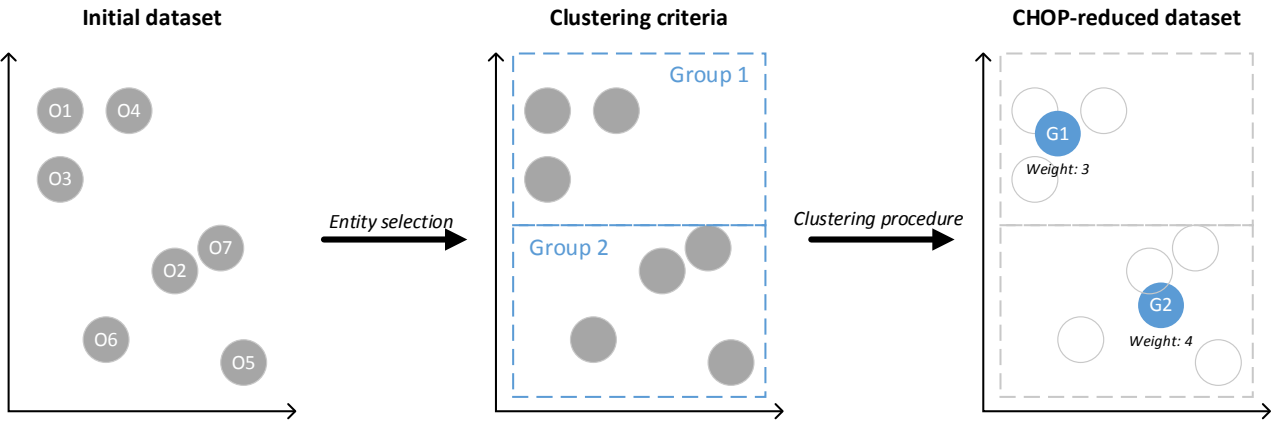


Figure 1 – Principal sketch of the data aggregation principle applied in the CHOP method. Operating points O_j are clustered and merged into CHOP groups G_j with aggregated weight factors.

Figure 2

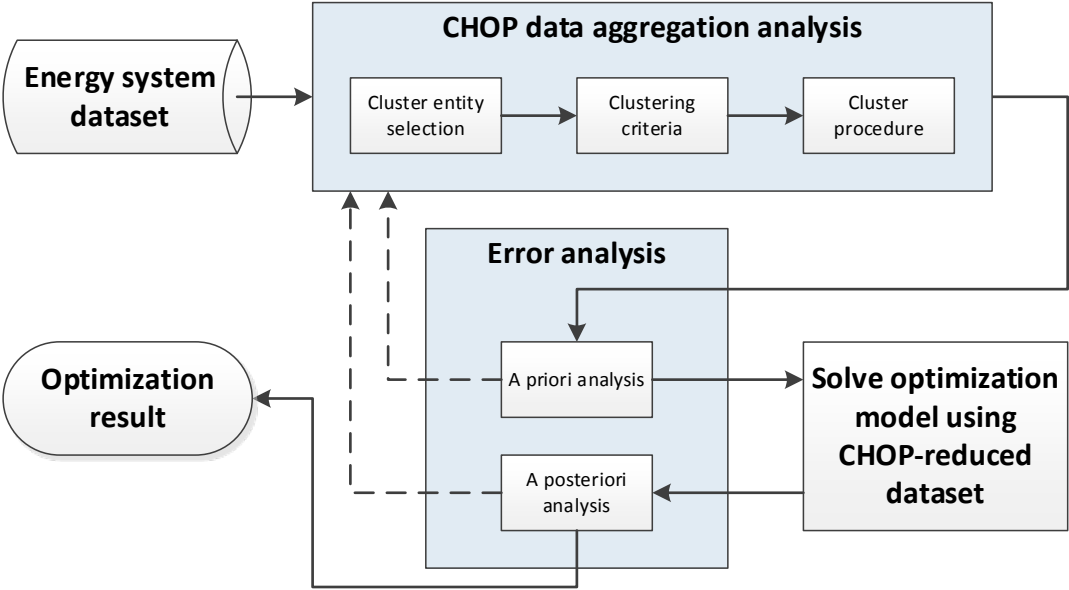


Figure 2 – The CHOP method procedure.

Figure 3

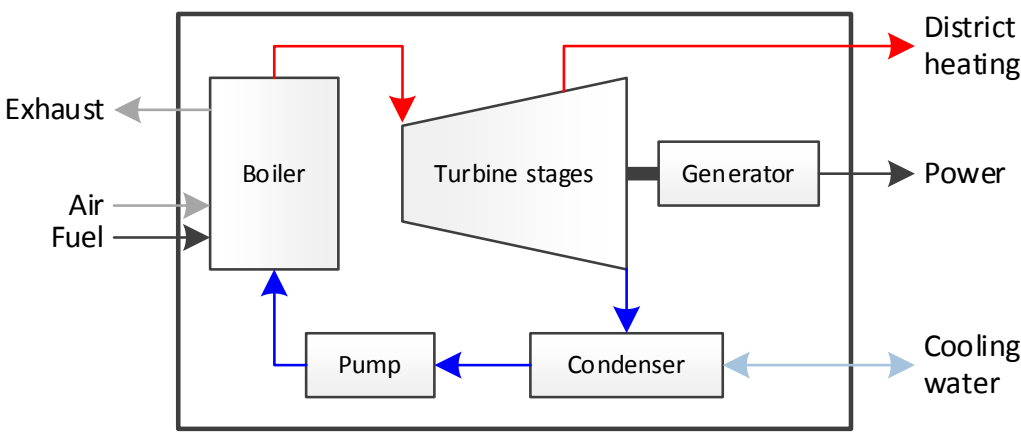


Figure 3 – Principal sketch of a Danish extraction-based CHP plant.

Figure 4

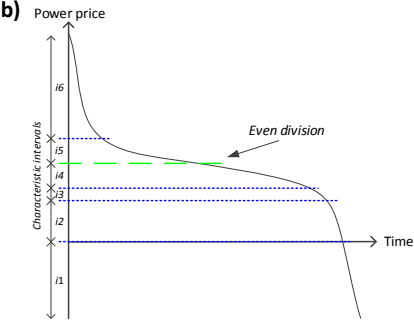
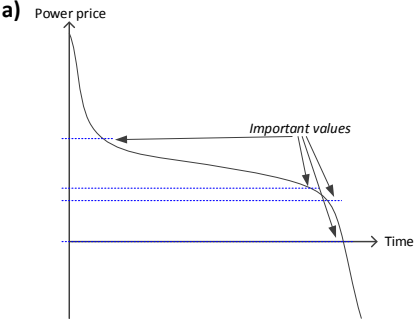
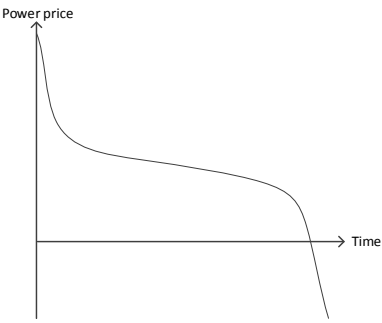


Figure 4 – Illustrative example of the suggested two-step approach for defining characteristic intervals based on the cumulative curve (left). Interval break points are set for a) Important values, and b) Even division. The characteristic intervals are indicated on the second axis in b).

Figure 5

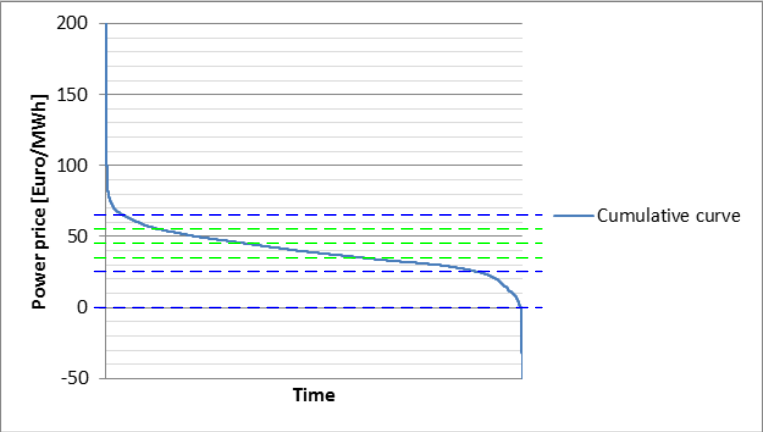


Figure 5 – Cumulative curve for the power price in West Denmark over the period 2010-01-01 – 2014-12-31, with interval break lines.

Figure 6

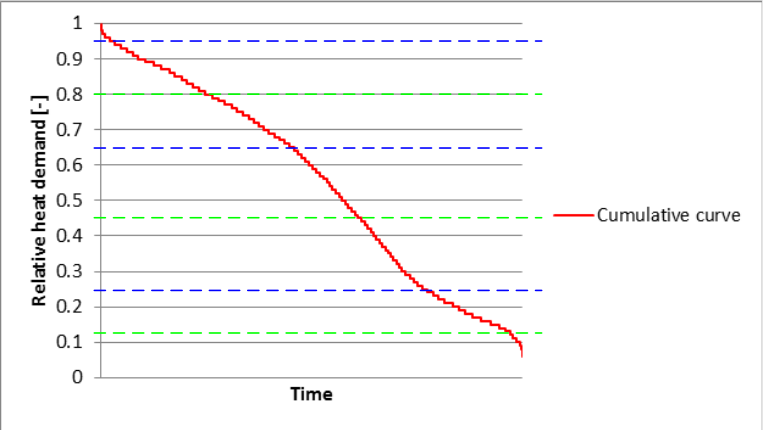


Figure 6 – Cumulative curve for the relative heat demand in Denmark over the period 2010-01-01 – 2014-12-31, with interval break lines.

Figure 7

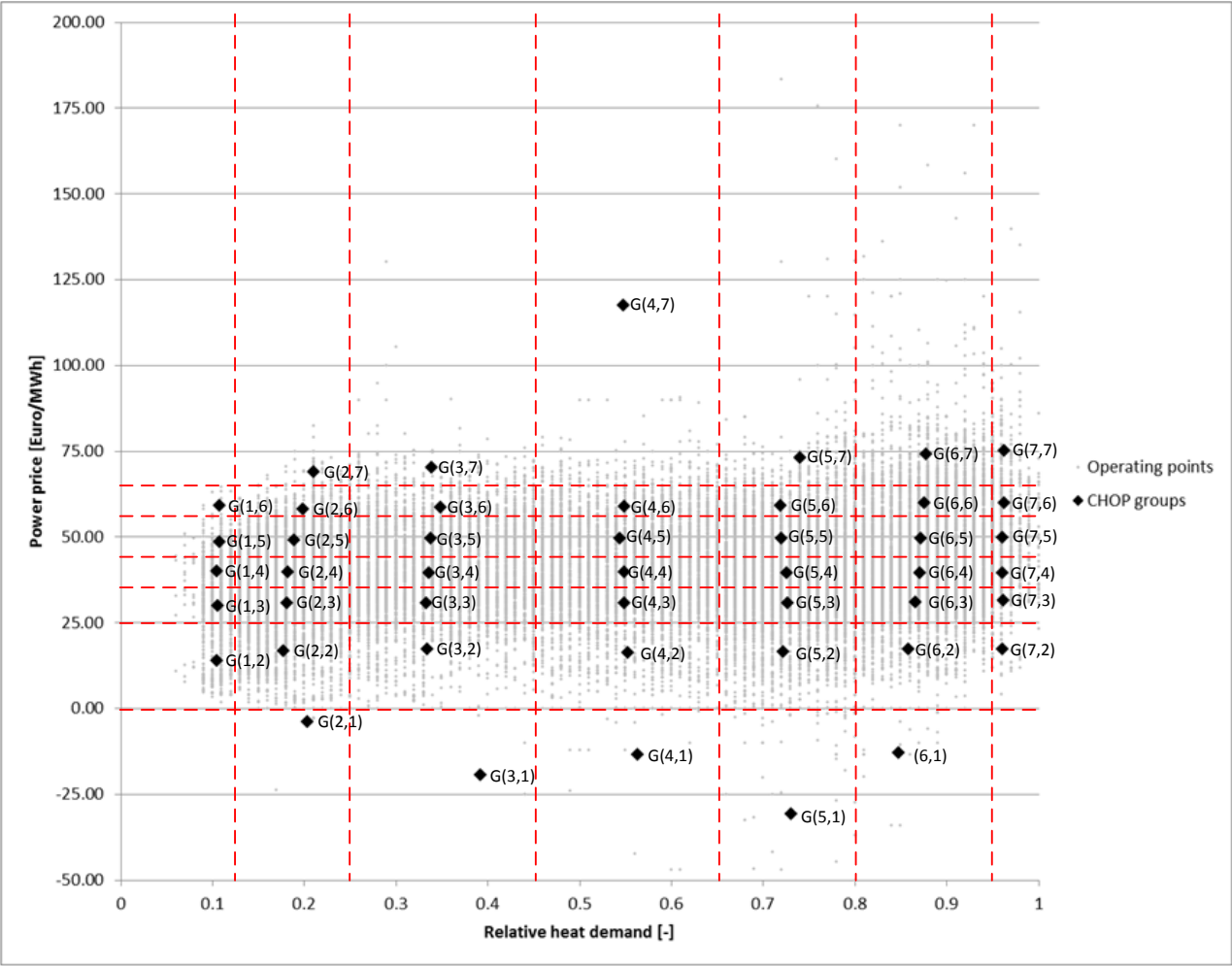


Figure 7 Caption

Figure 7 – Scatter diagram showing the reference operating points, characteristic interval breaks, and final CHOP groups. Notice that a small number of the reference operating points lies outside the power price boundaries of the diagram.

Figure 8

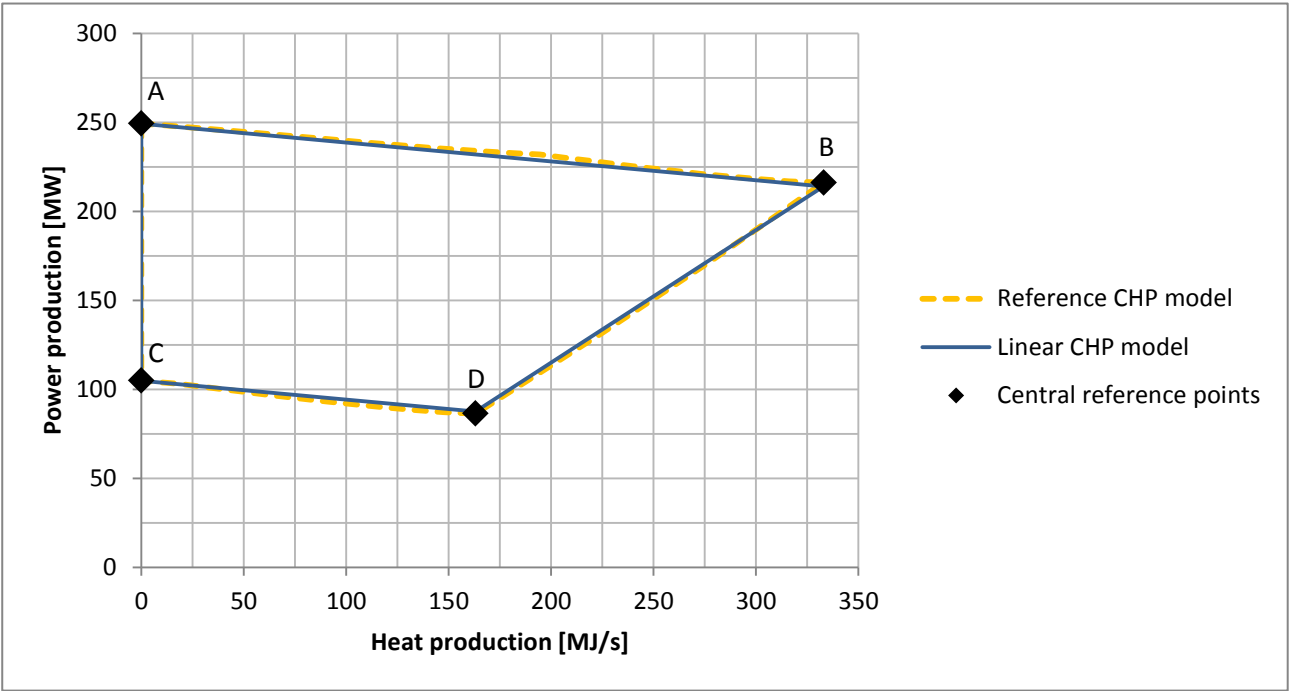


Figure 8 – Heat and power production range of the reference CHP plant model [43] and the developed linearized model. The outlined areas represent the feasible production points of the models. Four central operating points {A, B, C, D} are highlighted. Data for these operating points is presented in Table 6.

Figure 9

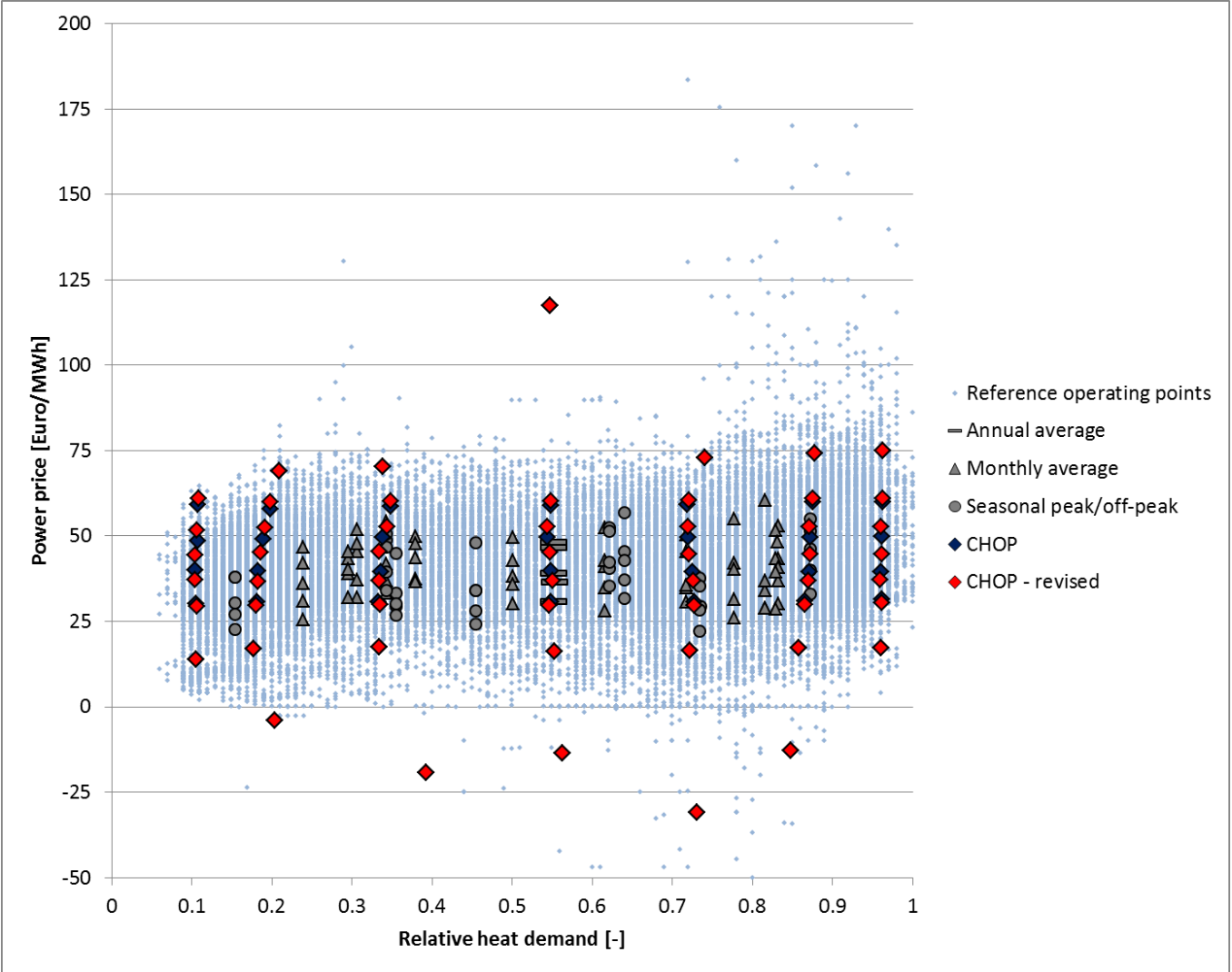


Figure 9 Caption

Figure 9 – Scatter diagram showing reference, annually averaged, monthly averaged, seasonal peak/off-peak, CHOP, and revised-CHOP operating points over the period 2010-01-01 – 2014-12-31. Notice that some of the CHOP and revised-CHOP operating points are overlapping.

Figure 10

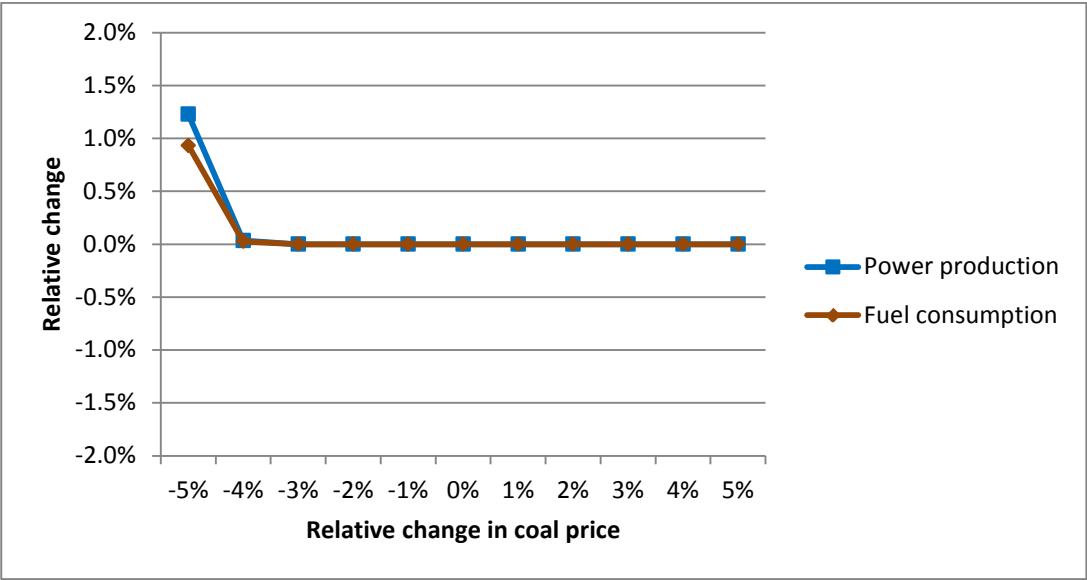


Figure 10 Caption

Figure 10 – Relative changes in optimized power production and fuel consumption as a function of relative changes in the coal price. Notice that heat production is unaffected by the coal price as it is constrained in the optimization model.

Figure 11

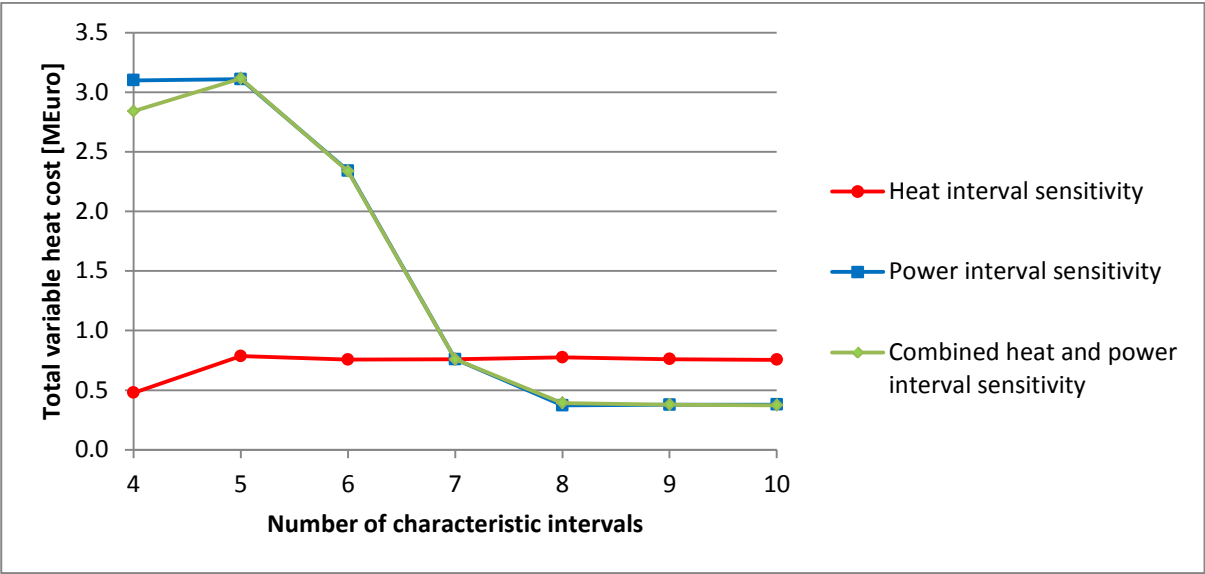


Figure 11 – Total variable heat cost sensitivity analysis.

Figure 12

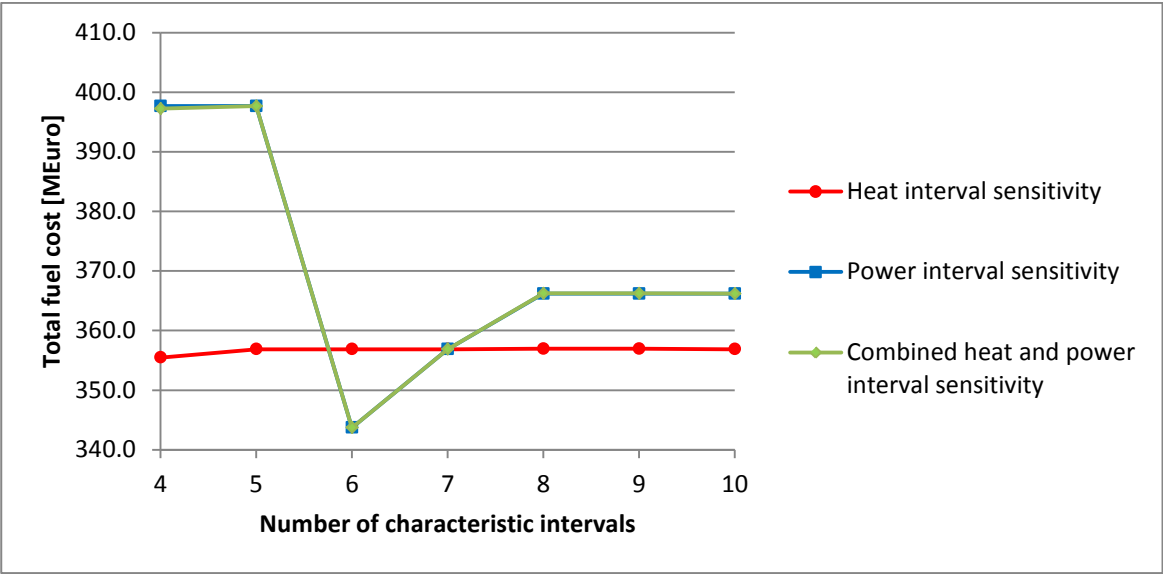


Figure 12 – Total fuel cost sensitivity analysis.

Figure 13

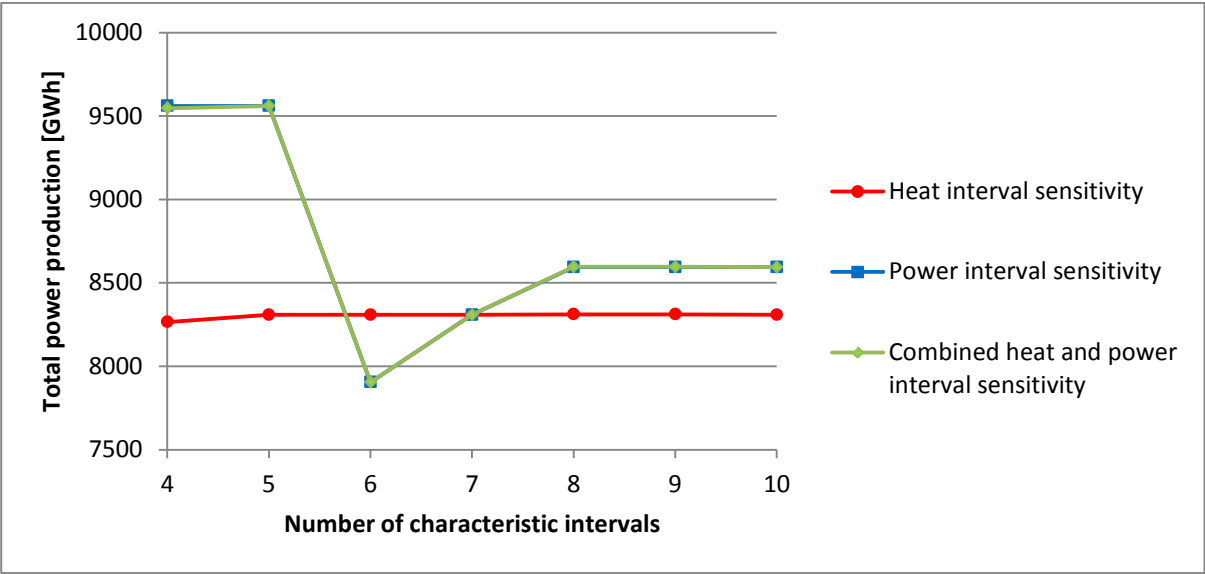


Figure 13 – Total power production sensitivity analysis.

Figure 14

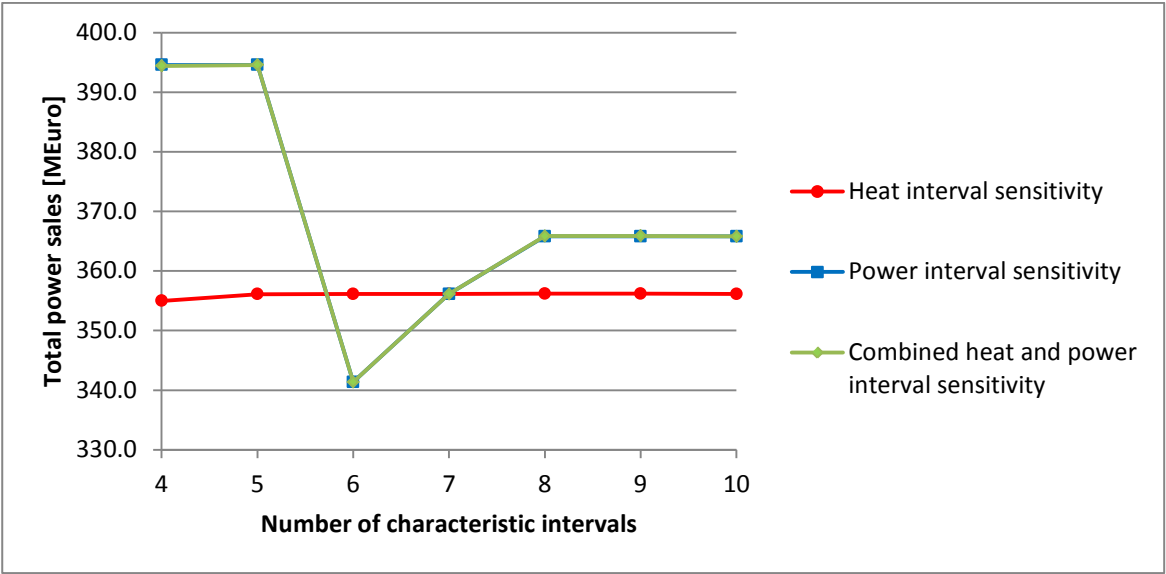


Figure 14 – Total power sales sensitivity analysis.

Figure 15

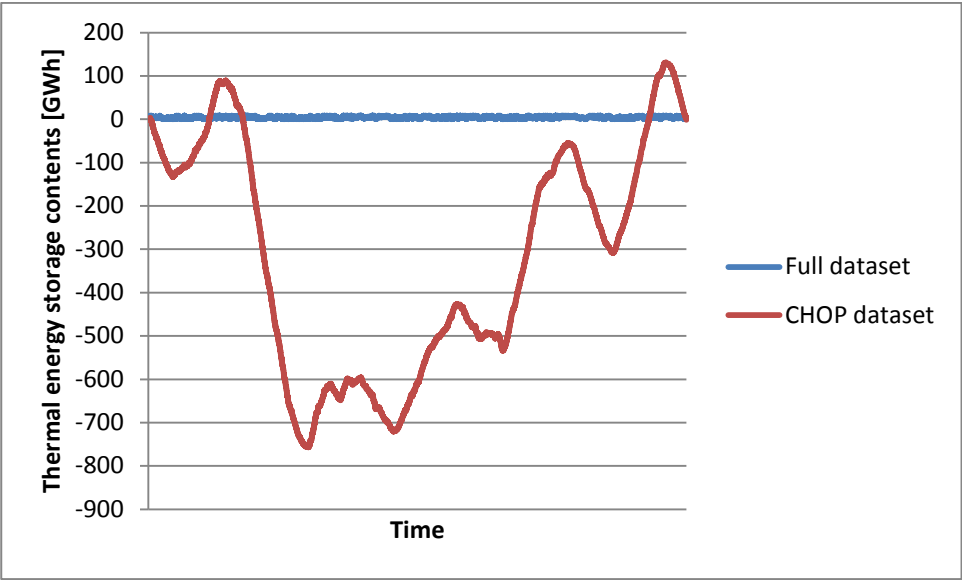


Figure 15 – Thermal energy storage contents over the 5-year period for the optimal solutions to problem (27) obtained using the full EOC dataset and the revised CHOP dataset.

Table 1

Table 1 – Characteristic power price intervals.

Power price interval number <i>i</i>	Smallest value [Euro/MWh]	Largest value [Euro/MWh]
1	$-\infty^a$	-0.01
2	0.00	24.99
3	25.00	34.99
4	35.00	44.99
5	45.00	54.99
6	55.00	64.99
7	65.00	∞^a

^a Notice that the intervals are defined as open towards the infinite to cover all feasible power prices

Table 2

Table 2 – Characteristic heat demand intervals.

Heat demand interval number <i>i</i>	Smallest value [-]	Largest value [-]
1	0.000	0.124
2	0.125	0.249
3	0.250	0.449
4	0.450	0.649
5	0.650	0.799
6	0.800	0.949
7	0.950	1.000

Table 3

Table 3 – Characteristics of the defined CHOP groups.

CHOP group characteristics							
Duration [h]	Power interval						
Heat interval	1	2	3	4	5	6	7
1	0	321	427	390	136	16	0
2	11	1178	2812	2327	1838	379	55
3	9	615	1808	1826	1739	640	178
4	22	717	1847	1828	1672	741	198
5	72	947	2380	2436	1649	803	273
6	30	582	2608	2932	1871	1158	903
7	0	46	262	442	272	217	211
Relative heat demand [-]							
1	-	0.105	0.106	0.104	0.107	0.108	-
2	0.204	0.178	0.181	0.183	0.189	0.199	0.210
3	0.392	0.334	0.333	0.336	0.338	0.348	0.339
4	0.563	0.553	0.548	0.549	0.544	0.549	0.547
5	0.731	0.721	0.727	0.726	0.720	0.719	0.740
6	0.848	0.858	0.866	0.871	0.872	0.875	0.878
7	-	0.961	0.961	0.960	0.961	0.963	0.963
Power price [Euro/MWh]							
1	-	13.91	30.06	40.14	48.52	59.09	-
2	-3.92	16.86	30.65	39.70	49.04	58.00	69.02
3	-19.24	17.43	30.77	39.43	49.58	58.53	70.32

4	-13.46	16.22	30.78	39.78	49.48	58.99	117.54
5	-30.81	16.58	30.73	39.54	49.58	59.13	72.97
6	-12.90	17.36	31.01	39.58	49.60	59.90	74.10
7	-	17.20	31.54	39.56	49.74	60.00	75.08

Table 4

Table 4 – CHOP group relative heat demand standard deviation, $\sigma_{\lambda_{heat}}$.

CHOP group $\sigma_{\lambda_{heat}}$ [-]							
Heat interval \ power interval	1	2	3	4	5	6	7
1	-	0.011	0.012	0.012	0.012	0.011	-
2	0.026	0.032	0.032	0.033	0.031	0.029	0.020
3	0.065	0.058	0.059	0.060	0.061	0.058	0.059
4	0.055	0.058	0.058	0.058	0.059	0.060	0.061
5	0.040	0.041	0.044	0.044	0.043	0.045	0.044
6	0.038	0.042	0.042	0.042	0.042	0.042	0.042
7	-	0.011	0.013	0.012	0.013	0.014	0.013

Table 5 – CHOP group power price standard deviation, $\sigma_{c_{power}}$.

CHOP group $\sigma_{c_{power}}$ [Euro/MWh] Heat interval \ power interval	1	2	3	4	5	6	7
1	-	6.57	2.70	2.80	2.37	3.14	-
2	6.35	6.45	2.63	2.90	2.76	2.67	3.61
3	21.67	6.64	2.66	2.89	2.82	2.82	7.49
4	16.79	6.91	2.70	2.87	2.78	2.82	293.62
5	55.98	7.23	2.64	2.87	2.91	2.75	14.17
6	16.10	6.42	2.54	2.78	2.86	3.07	13.46
7	-	4.61	2.31	2.83	2.96	2.87	11.07

Table 6 – Data on four central reference points {A, B, C, D} in the reference model of AVV1 [43], and their corresponding points {A, B*, C*, D*} in the linearized model of AVV1.*

Point, j	Load, λ	Back-pressure ratio, α	Power production, P_j [MW]	Heat production, Q_j [MJ/s]
A	1.0	0.0	249.3	0.0
A*	1.0	0.0	249.3	0.0
B	1.0	1.0	216.0	332.9
B*	1.0	1.0	213.9	332.9
C	0.4	0.0	104.9	0.0
C*	0.4	0.0	104.9	0.0
D	0.4	1.0	86.3	163.1
D*	0.4	1.0	87.5	163.1

Table 7

Table 7 – Optimization results obtained using the five different EOC datasets.

	Full dataset	Annually averaged	Monthly averaged	Seasonal peak/off-peak	CHOP- reduced
RESULTS					
Total variable heat cost, C_{heat} [MEuro]	0.38	8.53	8.02	5.96	0.76
Total power sales [MEuro]	368.06	369.51	376.62	370.41	356.12
Total fuel costs [MEuro]	368.44	377.81	384.64	376.38	356.88
PRODUCTION DATA					
Total heat production [GWh]	8,066	8,066	8,066	8,066	8,066
Total power production [GWh]	8,664	8,958	9,161	8,907	8,309
Total fuel consumption [GWh]	23,460	24,057	24,492	23,966	22,724
OPTIMIZATION PROBLEM					
Number of periods	43,824	5	60	40	46
Variables per period	2	2	2	2	2
Constraints per period	4	4	4	4	4

Table 8

Table 8 – Interval break points as a function of the number of intervals defined.

No. of intervals	4	5	6	7	8	9	10
Relative heat demand interval breaks [-]	0.25	0.25	0.25	0.125	0.125	0.125	0.125
	0.65	0.45	0.45	0.25	0.25	0.25	0.25
	0.95	0.65	0.65	0.45	0.38	0.38	0.35
		0.95	0.80	0.65	0.52	0.52	0.45
			0.95	0.80	0.65	0.65	0.55
				0.95	0.80	0.75	0.65
					0.95	0.85	0.75
						0.95	0.85
							0.95
Power price interval breaks [Euro/MWh]	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	25.00	25.00	25.00	25.00	25.00	12.50	8.00
	65.00	45.00	38.00	35.00	33.00	25.00	17.00
		65.00	52.00	45.00	41.00	33.00	25.00
			65.00	55.00	49.00	41.00	33.00
				65.00	57.00	49.00	41.00
					65.00	57.00	49.00
						65.00	57.00
							65.00

Table 9

Table 9 – Characteristics of the revised CHOP groups.

CHOP group characteristics								
Duration [h]	Power interval							
Heat interval	1	2	3	4	5	6	7	8
1	0	321	356	306	242	55	10	0
2	11	1178	2198	2111	1872	980	195	55
3	9	615	1383	1673	1400	1150	407	178
4	22	717	1402	1600	1483	1085	518	198
5	72	947	1824	2163	1565	1139	577	273
6	30	582	1953	2641	1776	1301	898	903
7	0	46	189	365	267	195	177	211
Relative heat demand [-]								
1	-	0.105	0.106	0.105	0.105	0.107	0.109	-
2	0.204	0.178	0.180	0.182	0.186	0.191	0.199	0.210
3	0.392	0.334	0.335	0.334	0.334	0.344	0.348	0.339
4	0.563	0.553	0.546	0.550	0.547	0.544	0.549	0.547
5	0.731	0.721	0.727	0.726	0.721	0.720	0.721	0.740
6	0.848	0.858	0.866	0.870	0.872	0.871	0.876	0.878
7	-	0.961	0.961	0.960	0.962	0.961	0.963	0.963
Power price [Euro/MWh]								
1	-	13.91	29.32	37.20	44.49	51.62	61.11	-
2	-3.92	16.86	29.73	36.73	45.20	52.51	60.05	69.02
3	-19.24	17.43	29.80	36.80	45.40	52.64	60.23	70.32

4	-13.46	16.22	29.77	36.83	45.20	52.59	60.34	117.54
5	-30.81	16.58	29.75	36.82	44.74	52.63	60.39	72.97
6	-12.90	17.36	30.03	36.98	44.76	52.59	61.08	74.10
7	-	17.20	30.56	37.11	44.58	52.75	60.95	75.08

Table 10 – Optimization results obtained using the CHOP and the revised CHOP EOC datasets.

	Full dataset	CHOP	CHOP-revised
RESULTS			
Total variable heat cost, C_{heat} [MEuro]	0.38	0.76	0.37
Total power sales [MEuro]	368.06	356.12	365.81
Total fuel costs [MEuro]	368.44	356.88	366.18
PRODUCTION DATA			
Total heat production [GWh]	8,066	8,066	8,066
Total power production [GWh]	8,664	8,309	8,594
Total fuel consumption [GWh]	23,460	22,724	23,317
OPTIMIZATION PROBLEM			
Number of periods	43,824	46	53
Variables per period	2	2	2
Constraints per period	4	4	4

Table 11 - Optimization results obtained from solving optimization problem (28) using the full EOC dataset and the revised CHOP dataset.

	Full dataset Problem (22)	Full dataset Problem (28)	CHOP-revised Problem (28)*
RESULTS			
Total variable heat cost, C_{heat} [MEuro]	0.38	-6.08	-8.06
Total power sales [MEuro]	368.06	372.50	357.04
Total fuel costs [MEuro]	368.44	366.42	348.97
PRODUCTION DATA			
Total heat production [GWh]	8,066	8,066	8,066
Total power production [GWh]	8,664	8,602	8,066
Total fuel consumption [GWh]	23,460	23,332	22,221
OPTIMIZATION PROBLEM			
Number of periods	43,824	43,824	53
Variables per period	2	2	2
Constraints per period	4	6	4

* Constraints (26) and (27) were slacked when solving optimization problem (28) using the CHOP-revised dataset.

Table 12 – Annually averaged EOC dataset, D_{AA} .

Year	Duration [h]	Power price, $c_{p,j}$ [Euro/MWh]	Relative heat demand, q_j [-]
2010	8760	46.48	0.553
2011	8760	47.96	0.553
2012	8784	36.33	0.554
2013	8760	38.98	0.553
2014	8760	30.67	0.553

Table 13 – Monthly averaged EOC dataset, D_{MA} , period duration.

Duration [h]	2010	2011	2012	2013	2014
January	744	744	744	744	744
February	672	672	696	672	672
March	744	744	744	744	744
April	720	720	720	720	720
May	744	744	744	744	744
June	720	720	720	720	720
July	744	744	744	744	744
August	744	744	744	744	744
September	720	720	720	720	720
October	744	744	744	744	744
November	720	720	720	720	720
December	744	744	744	744	744

Table 14 – Monthly averaged EOC dataset, D_{MA} , period power price.

Power price [Euro/MWh]	2010	2011	2012	2013	2014
January	43.29	52.89	37.01	40.77	30.26
February	43.45	51.75	48.35	39.40	28.74
March	42.09	55.14	31.51	40.33	26.05
April	41.11	52.33	34.76	42.82	28.13
May	41.73	54.35	36.06	36.82	33.34
June	45.49	51.99	37.21	47.74	31.88
July	46.81	42.20	25.55	36.24	31.02
August	43.28	45.42	39.01	40.17	32.11
September	49.86	47.79	37.40	43.67	36.58
October	49.48	42.76	38.11	35.90	30.13
November	50.45	45.45	34.91	35.60	30.78
December	60.50	33.97	36.86	28.80	28.99

Table 15 – Monthly averaged EOC dataset, D_{MA} , period relative heat demand.

Relative heat demand[-]	2010	2011	2012	2013	2014
January	0.83	0.83	0.83	0.83	0.83
February	0.83	0.83	0.83	0.83	0.83
March	0.78	0.78	0.78	0.78	0.78
April	0.62	0.62	0.62	0.62	0.62
May	0.34	0.34	0.34	0.34	0.34
June	0.31	0.31	0.31	0.31	0.31
July	0.24	0.24	0.24	0.24	0.24
August	0.30	0.30	0.30	0.30	0.30
September	0.38	0.38	0.38	0.38	0.38
October	0.50	0.50	0.50	0.50	0.50
November	0.72	0.72	0.72	0.72	0.72
December	0.82	0.82	0.82	0.82	0.82

Table 16 – Seasonal averaged peak/off-peak averaged EOC dataset, D_{SP} , period duration.

Duration [h]	2010	2011	2012	2013	2014
Winter, peak	1440	1440	1456	1440	1440
Winter, off-peak	720	720	728	720	720
Spring, peak	1470	1470	1470	1470	1470
Spring, off-peak	736	736	736	736	736
Summer, peak	1472	1472	1472	1472	1472
Summer, off-peak	736	736	736	736	736
Autumn, peak	1456	1456	1456	1456	1456
Autumn, off-peak	728	728	728	728	728

Table 17 – Seasonal averaged peak/off-peak averaged EOC dataset, D_{SP} , period power price.

Power price [Euro/MWh]	2010	2011	2012	2013	2014
Winter, peak	55.11	51.29	46.21	40.09	32.95
Winter, off-peak	37.58	35.48	29.29	28.49	22.15
Spring, peak	45.49	56.95	37.08	42.97	31.62
Spring, off-peak	33.96	47.97	28.15	33.94	24.33
Summer, peak	48.85	50.75	39.44	46.76	34.01
Summer, off-peak	37.87	37.91	22.78	30.43	26.98
Autumn, peak	52.45	51.37	40.53	42.45	35.35
Autumn, off-peak	44.88	33.19	29.42	30.19	26.71

Table 18 – Seasonal averaged peak/off-peak averaged EOC dataset, D_{SP} , period relative heat demand.

Relative heat demand[-]	2010	2011	2012	2013	2014
Winter, peak	0.87	0.87	0.87	0.87	0.87
Winter, off-peak	0.73	0.73	0.73	0.73	0.73
Spring, peak	0.64	0.64	0.64	0.64	0.64
Spring, off-peak	0.45	0.45	0.45	0.45	0.45
Summer, peak	0.34	0.34	0.34	0.34	0.34
Summer, off-peak	0.15	0.15	0.15	0.15	0.15
Autumn, peak	0.62	0.62	0.62	0.62	0.62
Autumn, off-peak	0.36	0.36	0.36	0.36	0.36